# Tensor feature hallucination for few-shot learning

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# What is few-shot learning

• Why is it important?









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### **Contributions**

#### Previous state of the art

- Meta-learning:
- Transfer learning
- Domain adaptation
- Synthetic data generation

#### Contributions

- Exploit the spatial properties of tensor features
- Introduce a novel loss function that is simpler than the other state of the art
- Provide state of the art performance in three benchmark datasets

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### **Problem formulation and definitions**

#### Representation learning

- Base class dataset:  $D_{\text{base}} := \{(x_i, y_i)\}_{i=1}^I$  where  $y_i \in C_{\text{base}}$
- Train embedding network  $f_{\theta}: \mathcal{X} \to \mathbb{R}^{d \times h \times w}$  on  $D_{\text{base}}$
- $ar{f}_{ heta}: \mathcal{X} o \mathbb{R}^d$  denotes  $f_{ heta}$  followed by global average pooling (GAP)

#### Inference stage

- Novel class dataset  $D_{\text{novel}}$  with  $C_{\text{novel}}$  disjoint from  $C_{\text{base}}$
- ullet Sample a support set S and a query set Q from  $D_{
  m novel}$
- ullet S consists of N classes with K labeled examples per class
- Given S and  $f_{\theta}$ , classify examples from Q

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### Representation learning

• 1st stage: train the backbone network using standard cross-entropy

$$L(D_{\text{base}}; \theta, \phi) := \sum_{i=1}^{I} L_{\text{CE}}(c_{\phi}(\bar{f}_{\theta}(x_i)), y_i) + R(\phi)$$
 (1)

2nd stage: adopt a self-distillation process

$$L_{\text{KD}}(D_{\text{base}}; \theta', \phi') := \alpha L(D_{\text{base}}; \theta', \phi') + \beta \text{KL}(c_{\phi'}(\bar{f}_{\theta'}(x_i)), c_{\phi}(\bar{f}_{\theta}(x_i)))$$
(2)

### Meta-training tensor hallucinator

- ullet Meta-training stage: sample episodes of S from  $D_{\mathrm{base}}$
- Pre-trained network  $f_{\theta}: \mathcal{X} \to \mathbb{R}^{d \times h \times w}$  maps images to tensors
- Class prototype tensors:

$$p_j := \frac{1}{K} \sum_{i=1}^K f_{\theta'}(x_i^j)$$

- Conditioner h maps prototypes to class-conditional vectors  $s_i := h(p_i) \in \mathbb{R}^{d'}$
- Generator maps to  $g(z; s_i) \in \mathbb{R}^{d \times h \times w}$  where  $z \sim \mathcal{N}(\mathbf{0}, I_k)$
- Jointly trained by:

$$L_{\text{hal}}(X; h, g) = \frac{1}{MN} \sum_{i=1}^{N} \sum_{m=1}^{M} \|g(z_m; h(p_j)) - p_j\|^2$$

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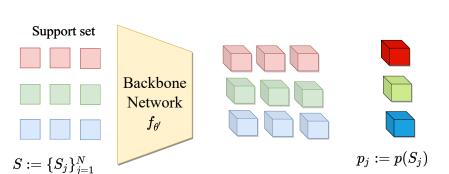
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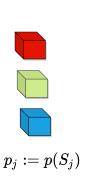
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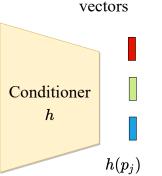
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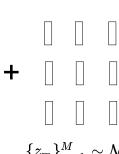
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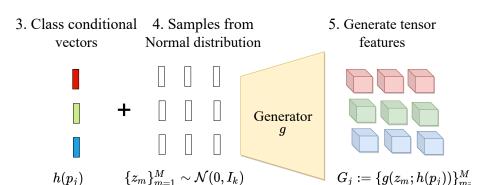
- 2. Tensor prototypes
- 3. Class conditional
- 4. Samples from Normal distribution



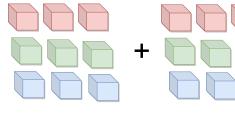


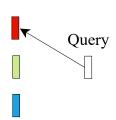


$$\{z_m\}_{m=1}^M \sim \mathcal{N}(0,I_k)$$



- 5. Generate tensor features
- 6. Augment Support tensors
- 7. GAP and prototype classification





$$G_j := \{g(z_m; h(p_j))\}_{m=1}^M$$

# **Experimental results**

Mrmyon		an Non	CHD	
МЕТНОО	miniIMAGENET		CUB	
	1-shot	5-shot	1-shot	5-shot
Dual TriNet [Chen et al. 2019]	58.80±1.37	$76.71_{\pm 0.69}$	69.61	84.10
IDeMe-Net [Chen et al. 2019]	$59.14 \pm 0.86$	$74.63 \pm 0.74$	_	_
AFHN [Li <i>et al.</i> 2020]	$62.38 \scriptstyle{\pm 0.72}$	$78.16{\scriptstyle\pm0.56}$	$70.53{\scriptstyle\pm1.01}$	$83.95{\scriptstyle\pm0.63}$
VI-Net [Luo <i>et al</i> . 2021]	61.05	78.60	74.76	86.84
Baseline (1)	56.81±0.81	78.31±0.59	67.14±0.89	86.22±0.50
Baseline-KD (2)	$59.62 \scriptstyle{\pm 0.85}$	$79.31{\scriptstyle\pm0.62}$	$70.85{\scriptstyle\pm0.90}$	$87.64{\scriptstyle \pm 0.48}$
VFH (ours)	$61.88{\scriptstyle\pm0.85}$	$79.63{\scriptstyle\pm0.61}$	$75.44{\scriptstyle\pm0.85}$	$87.82{\scriptstyle\pm0.47}$
TFH (ours)	$64.49{\scriptstyle\pm0.84}$	$79.94{\scriptstyle\pm0.60}$	$75.66{\scriptstyle \pm 0.85}$	$88.39{\scriptstyle\pm0.49}$
TFH-ft (ours)	<b>65.07</b> ±0.82	$80.81 \scriptstyle{\pm 0.61}$	<b>75.76</b> ±0.83	<b>88.60</b> ±0.47

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# Thank you!

https://github.com/MichalisLazarou https://avrithis.net http://www.commsp.ee.ic.ac.uk/~tania/